

**Today's Learning:**

Solving Simultaneous Equations by elimination.

$$\textcircled{1} \quad T + B = 6$$

$$\textcircled{2} \quad T - B = 4$$

Add

$$\hline$$

$$2T = 10$$

$$T = 5$$

Use  $\textcircled{1}$   $T + B = 6$

$$5 + B = 6$$

$$-5 \quad -5$$

$$B = 1$$

Solving by elimination:

①  $2y + x = 5$

②  $4y - x = 7$

Add

$$6y = 12$$

$$y = 2$$

use ①  $2y + x = 5$

$$4 + x = 5$$

$$\begin{array}{r} -4 \\ 4 + x = 5 \\ \hline x = 1 \end{array}$$

$$\begin{array}{l} x = 1 \\ y = 2 \end{array}$$

$$4b + 2c = 50 \quad \text{①}$$

$$2b + 2c = 30 \quad \text{②}$$

①  $4b + 2c = 50$

$$-1 \times \text{②} \quad -2b - 2c = -30$$

---

Add

$$2b = 20$$

$$b = 10 \quad \checkmark$$

use ①  $4b + 2c = 50$

$$40 + 2c = 50$$

$$\begin{array}{r} -40 \\ 40 + 2c = 50 \\ \hline 2c = 10 \end{array}$$

$$2c = 10$$

$$c = 5 \quad \checkmark$$

$$8p + 6q = 2 \quad \textcircled{1}$$

$$8p + 5q = -1 \quad \textcircled{2}$$

$$\begin{array}{r} \textcircled{1} \quad 8p + 6q = 2 \\ -1 \times \textcircled{2} \quad -8p - 5q = 1 \\ \hline \qquad \qquad \qquad q = 3 \quad \checkmark \end{array} \quad \text{Add}$$

$$\begin{array}{l} \text{use } \textcircled{1} \quad 8p + 6q = 2 \\ \qquad \qquad 8p + 18 = 2 \\ \qquad \qquad -18 \quad -18 \\ \qquad \qquad 8p = -16 \\ \qquad \qquad p = -2 \quad \checkmark \end{array}$$

$$6b + a = 5 \quad \textcircled{1}$$

$$-6b + 4a = 5 \quad \textcircled{2}$$

$$\hline \text{Add}$$

$$5a = 10$$

$$a = 2$$

use  $\textcircled{1}$

$$6b + 2 = 5$$

$$-2 \quad -2$$

$$6b = 3$$

$$\div 6 \quad \div 6$$

$$b = \frac{3}{6} = \frac{1}{2}$$

$$5a + 4b = 42 \quad (1)$$

$$2a + 4b = 12 \quad (2)$$

$$-1 \times (1) \quad -5a - 4b = -42$$

$$(2) \quad 2a + 4b = 12$$

$$\hline 3a = -30 \quad \text{Add}$$

$$a = -10 \quad \checkmark$$

$$\text{use (2)} \quad -20 + 4b = 12$$

$$+20 \quad +20$$

$$4b = 32$$

$$\div 4 \quad \div 4$$

$$b = 8 \quad \checkmark$$

$$4b + c = 21 \quad (1)$$

$$2b + 3c = 13 \quad (2)$$

$$-3 \times (1) \quad -12b - 3c = -63$$

$$(2) \quad 2b + 3c = 13$$

$$\hline -10b = -50 \quad \text{Add}$$

$$b = 5 \quad \checkmark$$

$$\text{use (2)} \quad 2b + 3c = 13$$

$$10 + 3c = 13$$

$$-10 \quad -10$$

$$3c = 3 \quad \checkmark$$

$$c = 1$$

$$6a + 2b = 5 \quad (1)$$

$$2a + 10b = 11 \quad (2)$$

$$(1) \quad 6a + 2b = 5$$

$$-3 \times (2) \quad -6a - 30b = -33$$


---


$$-28b = -28$$

use (1)  $b = 1$  ✓

$$6a + 2b = 5$$

$$6a + 2 = 5$$

$$-2 \quad -2$$

$$6a = 3$$

$$\div 6 \quad \div 6$$

$$a = \frac{3}{6} = \frac{1}{2} \quad \checkmark$$

$$2a + 3b = 40 \quad (1)$$

$$3a + 2b = 35 \quad (2)$$

$$2 \times (1) \quad 4a + 6b = 80$$

$$-3 \times (2) \quad -9a - 6b = -105$$

---


$$-5a = -25 \quad \text{Add}$$

$$a = 5$$

use (1)  $2a + 3b = 40$

$$10 + 3b = 40$$

$$-10 \quad -10$$

$$3b = 30$$

$$\underline{\underline{b = 10}}$$

## Solving Simultaneous Equations

- ★ Label the equations
- ★ Multiply each equation so you can cancel something out
- ★ Add the equations together
- ★ Solve
- ★ Substitute to find the other unknown

e.g. 1)  $7b - 5c = 35$  ①  
 $9b - 4c = 45$  ②

$$\begin{array}{r}
 -4 \times \textcircled{1} \quad -28b + 20c = -140 \\
 5 \times \textcircled{2} \quad 45b - 20c = 225 \\
 \hline
 \text{Add}
 \end{array}$$

$$\begin{array}{r}
 17b = 85 \\
 \div 17 \quad \div 17 \\
 b = 5
 \end{array}$$

use ①  $7b - 5c = 35$

$$\begin{array}{r}
 35 - 5c = 35 \\
 -35 \quad -35 \\
 \hline
 -5c = 0 \\
 c = 0
 \end{array}$$

$$2) \quad 2x + 3y = 7 \quad \textcircled{1}$$

$$4x + 5y = 12 \quad \textcircled{2}$$

$$-2 \times \textcircled{1} \quad -4x - 6y = -14$$

$$\textcircled{2} \quad 4x + 5y = 12$$

$$+ \quad \hline$$

$$-y = -2$$

$$y = 2$$

$$\text{use } \textcircled{1} \quad 2x + 3y = 7$$

$$2x + 6 = 7$$

$$-6 \quad -6$$

$$2x = 1$$

$$x = \frac{1}{2}$$

### Today's Learning:

To practise exam type questions on simultaneous equations.

$$4a + 3b = 22 \quad \textcircled{1} \times 4$$

$$12a - 4b = 40 \quad \textcircled{2} \times 3$$

$$4 \times \textcircled{1} \quad 16a + 12b = 88$$

$$3 \times \textcircled{2} \quad 36a - 12b = 120$$

$$\begin{array}{r} 16a + 12b = 88 \\ 36a - 12b = 120 \\ \hline 52a = 208 \\ \div 52 \qquad \div 52 \\ a = 4 \end{array} \quad \text{Add}$$

use  $\textcircled{2}$   $12a - 4b = 40$

$$48 - 4b = 40$$

$$\begin{array}{r} 48 - 4b = 40 \\ -48 \qquad -48 \\ \hline -4b = -8 \\ \div -4 \qquad \div -4 \\ b = 2 \end{array}$$

$$\begin{array}{l} a = 4 \\ b = 2 \end{array}$$

### Exam Questions

Two burgers and a milkshake cost £8.40. Three burgers and two milkshakes cost £13.55. By forming a pair of simultaneous equations, find the cost of burgers and milkshakes.

$$2b + m = 8.4 \quad \textcircled{1}$$

$$3b + 2m = 13.55 \quad \textcircled{2}$$

$$-2 \times \textcircled{1} \quad -4b - 2m = -16.8$$

$$\textcircled{2} \quad 3b + 2m = 13.55$$

$$\begin{array}{r} -4b - 2m = -16.8 \\ 3b + 2m = 13.55 \\ \hline -b = -3.25 \end{array} \quad \text{Add}$$

$$b = 3.25$$

use  $\textcircled{1}$   $2b + m = 8.4$

$$2 \times 3.25 + m = 8.4$$

$$6.5 + m = 8.4$$

$$m = 1.9$$

Burger £3.25

Milkshake £1.90