## Percentages

## Learning objectives

By the end of this topic, you should be able to:

- calculate compound interest;
- calculate appreciation;
- calculate depreciation;
- reverse percentages;

Key Words

Appreciation is when a value increases.
Depreciation is when a value decreases.
Before, originally, at the start-backward percentages

## Example 1

$£ 5000$ is invested in a bank for 10 years. $2 \%$ interest is paid annually. Calculate the compound interest at the end of 10 years.

## Example 2

A house was valued at $£ 125,000$ and sold 2 years later.
It increased in value by $4 \%$ in the first year and by $7 \%$ in the second year.
Calculate the value of the house when it was sold.

## Example 3

$£ 640$ is placed in a bank for 4 years. $3.5 \%$ interest is paid annually. How much is in the bank at the end of the 4 years?

## Example 4

The sale price of a bicycle after it has been reduced by $20 \%$ is $£ 135 \cdot 20$.
Calculate the original price of the bike.

Q11: A Painting which cost $£ 500000$ appreciated by $12 \%$ last year and $9 \%$ this year. Calculate the value of the painting now.

Q12: A car worth $£ 15000$ loses $8 \%$ of its value a year.
What is it worth by the end of 7 years?
Give your answer to the nearest penny.

Q13: A motorbike was bought for $£ 3200$.
It depreciated by $20 \%$ in the first year and $12 \%$ in the second year.
How much is it worth now? Give your answer to the nearest pound.

Q14: A collector bought an antique vase for $£ 600$.
The vase increases in value by $3 \%$ in the first year. It decreased in value by $2 \%$ in the second year. It decreased in value by $3 \%$ in the third year.
What is the vase worth after 3 years?
Give your answer to the nearest penny.

## Q16: Appreciation

An antique valued at $£ 3541$ appreciates by $11 \%$.
What is it worth now? Give your answer to the nearest penny.

## Q17: Appreciation

A house was valued at $£ 215000$ and sold 2 years later.
In the first year it increased in value by $24 \%$ and $17 \%$ in the second year.
Calculate the value of the house when it was sold. Give your answer to the nearest pound.

Q18: Depreciation
A car valued at $£ 2027$ depreciates by $10 \%$.
What is it worth now? Give your answer to the nearest penny.

## Q19: Depreciation

A yacht was bought new for $£ 86000$.
Over the course of 3 years it depreciated by $8 \%, 12 \%$ and $17 \%$.
Calculate the value of the yacht now. Give your answer to the nearest pound.

Q20: Increase/Decrease by a Percentage
A collector bought an antique vase for $£ 400$.
The vase increases in value by $3 \%$ in the first year.
It decreases in value by $4 \%$ in the second year.
It decreases in value by $3 \%$ in the third year.
What is the vase worth (in $£$ 's) after 3 years? Give your answer to the nearest penny.

Q23: Undoing a percentage increase
The population of an island increased by $16 \%$ this year to 82592 .
Calculate the population on the island last year. Give your answer to the nearest whole number.

Q24: Undoing a percentage decrease
A school role has dropped this session by $10 \%$ to 1134.
Calculate the school role last session. Give your answer to the nearest whole number.

Q25: Undoing percentages
The Smith's gas bill was $£ 816.96$ this year.
a) This was $20 \%$ increase on last year. How much did they pay last year? Give your answer to the nearest penny.
b) Last year's bill was $8 \%$ less than the previous year. How much did they pay for gas the previous year? Give your answer to the nearest penny.

## Answers

Q11: £ 610400
Q12: $£ 8367.70$
Q13: £ 2253
Q14: $£ 587.47$

Q16: £3930.51
Q17: $£ 311922$
Q18: $£ 1824.30$
Q19: $£ 57789$
Q20: £383•65

Q23: $71200(82592 \div 1 \cdot 16)$
Q24: $1260(1134 \div 0 \cdot 90)$
Q25:
a) $£ 680 \cdot 80$
b) $£ 740 \cdot 00$

## Exam Questions

1. A TV is reduced by $15 \%$ in a sale. It originally cost $£ 600$. How much does it cost now?
2. A house was valued at $£ 180000$. It appreciated in value by $2.4 \%$ in the first year. Depreciated in $1.3 \%$ in the second year. How much was the house worth at the end of the second year?
3. The number of bacteria in a petri dish is increasing at a rate of $3 \%$ every hour. If there are 12000 bacteria at the start then how many will there be in 4 hours?
4. A bank offers interest at a rate of $3.8 \%$ per annum on savings. Calculate the compound interest on an investment of £600 over three years.
5. A house appreciated in value by $2 \%$ over the course of a year. At the end of the year it was worth $£ 117$ 300. How much was the house worth at the start of the year?
