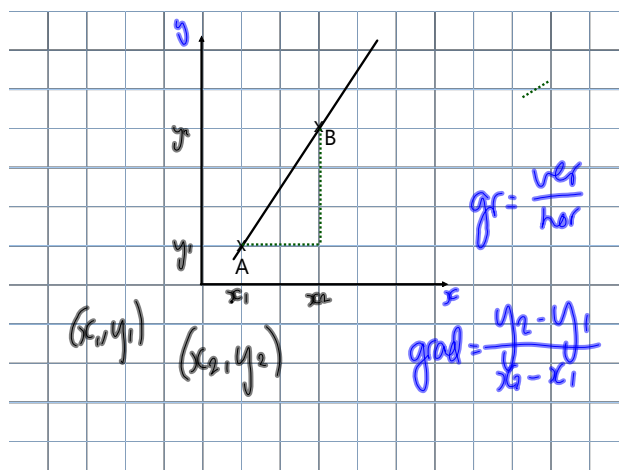


**Today's Learning:**

To calculate the gradient of a straight line using a formula.



**Gradient of a Straight Line** 23/1/18

The gradient of a line can be calculated by using

$$\frac{\text{vertical distance}}{\text{horizontal distance}}$$

Or, given coordinates of points on the line  $(x_1, y_1)$  and  $(x_2, y_2)$ , we can use:

$$\text{gradient} = \frac{y_2 - y_1}{x_2 - x_1}$$

**Parallel** lines have the same gradient.

**E.g.** Find the gradient of the straight line that passes through

- 1)  $(4, 4)$  and  $(6, 8)$ .  $gr = \frac{8-4}{6-4} = \frac{4}{2} = 2$
- 2)  $(-4, -3)$  and  $(2, 10)$ .  $gr = \frac{10 - (-3)}{2 - (-4)} = \frac{13}{6}$

Positive gradients:



Negative gradients:



**Without a calculator**, find the **gradient** of the straight line joining these points:

- |                                   |                   |
|-----------------------------------|-------------------|
| 1) $(-1, 3)$ and $(-2, 10)$       | 1) -7             |
| 2) $(-1, -5)$ and $(-2, -2)$      | 2) -3             |
| 3) $(3, -5)$ and $(5, -6)$        | 3) $-\frac{1}{2}$ |
| 4) $(2.5, 6)$ and $(3.5, 7.5)$    | 4) 1.5            |
| 5) $(-3.7, 4.5)$ and $(3.5, 6.5)$ | 5) $\frac{5}{18}$ |
| 6) $(2.2, 1.4)$ and $(-0.2, 2.2)$ | 6) $-\frac{1}{3}$ |

ANSWERS

★ If points are **collinear**, they all lie on the same straight line. (To prove collinearity, two straight lines must share a point and have the same gradient).

**e.g.** If  $A(-4, -2)$ ,  $B(-1, 1)$  and  $C(8, k)$  are collinear, find the value of  $k$ .

$$\text{grad}_{AB} = \frac{1 - (-2)}{-1 - (-4)} = \frac{3}{3} = 1$$

$$\text{grad}_{BC} = 1 = \frac{k - 1}{8 - (-1)}$$

$$1 = \frac{k - 1}{9}$$

$$9 = k - 1$$

$$10 = k$$

★ To prove collinearity of  $A, B$  and  $C$ , show  $AB$  grad =  $BC$  grad and state  $AB$  and  $BC$  both share point  $B$ .

