

Starter in Honour of St Andrews' Day

Answer

41700 Adult Tickets



Scotland have lined up a friendly match at Hampden against a Mathematical team from Spain: Real Mathdrid.

A decent crowd of 50,000 fans attend, as the tickets were only £20 for adults and £8 for kids. The SFA announce that they took £900,400 but won't reveal how many ticket sales were adult ones.

Can you work this out?

Similar Figures

Today we are learning...

What similar figures are and how to identify them.

I will know if I have been successful if...

I understand what a similar figure is.

I can find the scale factor of the enlargement or reduction.

I know how to check if two figures are similar.

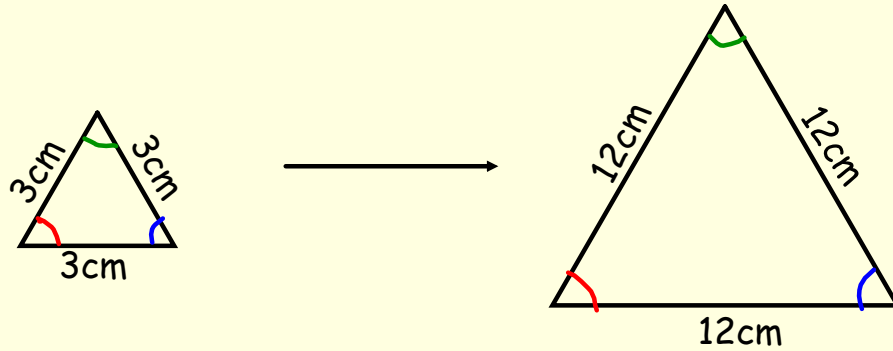


Similar Figures

Two shapes can be called similar if:

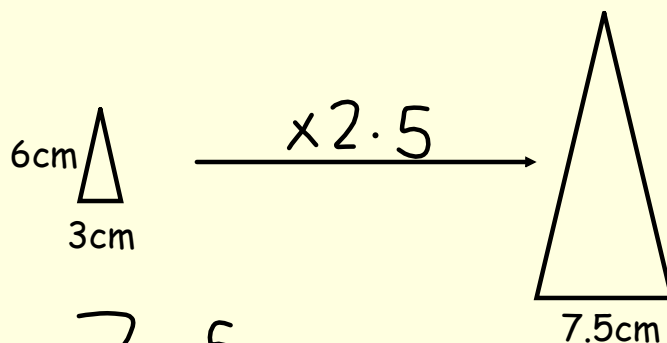
Their corresponding angles are equal.

Their corresponding sides are in the same ratio.



Scale Factor

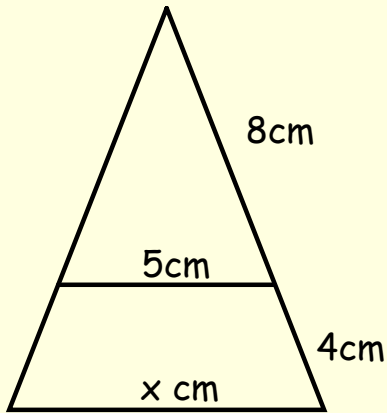
$$\text{Scale Factor} = \frac{\text{new}}{\text{old}}$$



$$SF = \frac{7.5}{3} = 2.5$$

Example 1

The two triangles are similar. Find the missing length x .



$$SF = \frac{\text{new}}{\text{old}}$$

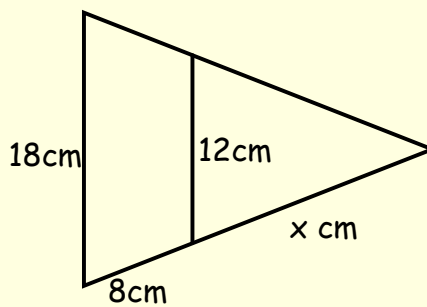
$$= \frac{12}{8} = \frac{3}{2} = 1.5$$

$$x = 5 \times 1.5$$

$$= 7.5 \text{ cm}$$

Example 2

The two triangles are similar. Find the missing length x .



$$SF = \frac{\text{new}}{\text{old}}$$

$$= \frac{3}{2}$$

$$\frac{3}{2}x = x + 8$$

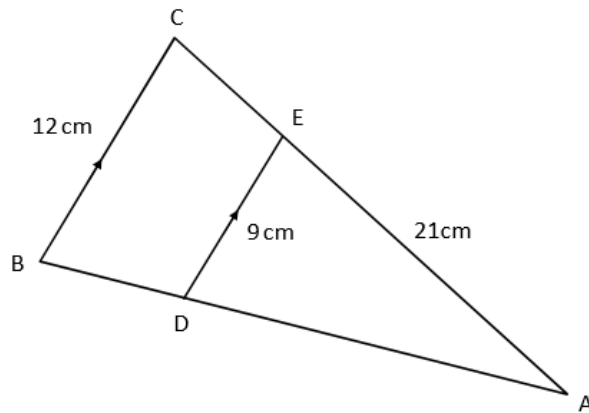
$$3x = 2x + 16$$

$$x = 16 \text{ cm}$$

Starter

1) In the diagram below triangles ABC and ADE are **mathematically similar**.

BC = 12 cm, DE = 9 cm and AE = 21 cm.



Find the length of CE.

2) Find the discriminant of $y = 2x^2 + 5x - 9$

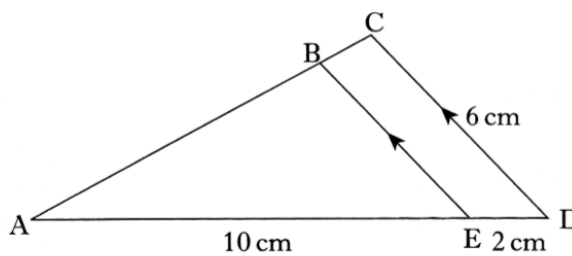
Example 1

Triangles ABE and ACD with some of their measurements are shown opposite.

Triangle ABE is similar to triangle ACD.

Calculate the length of BE.

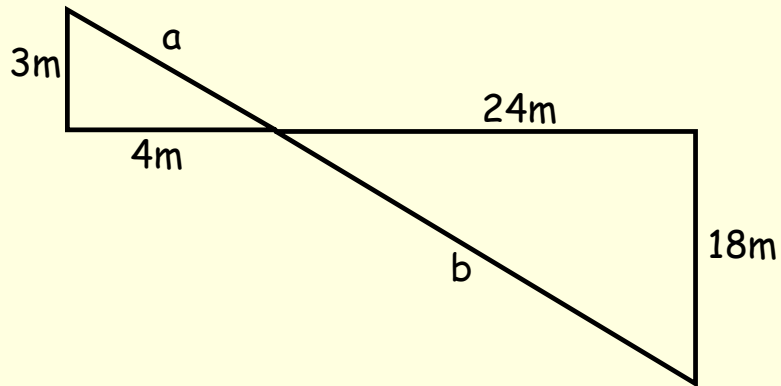
Do not use a scale drawing.



3 KU

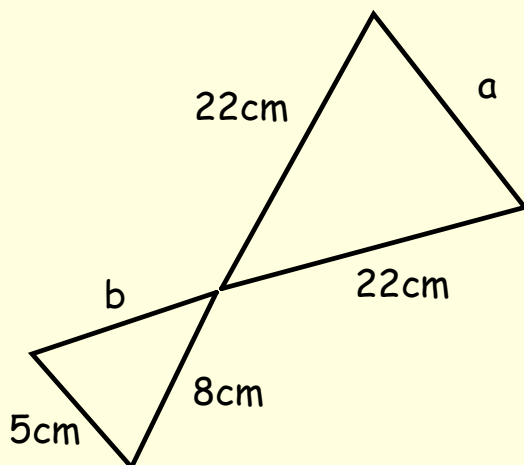
Example 2

The two triangles are similar. Find the missing lengths a and b .



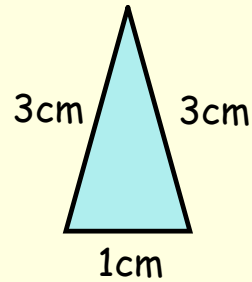
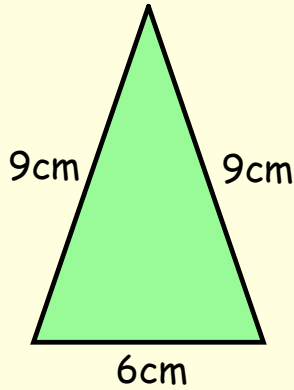
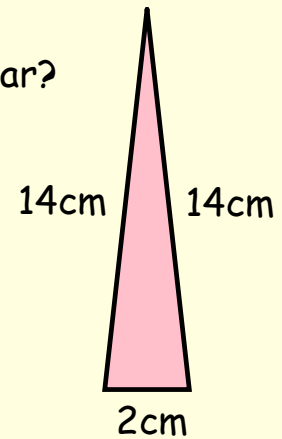
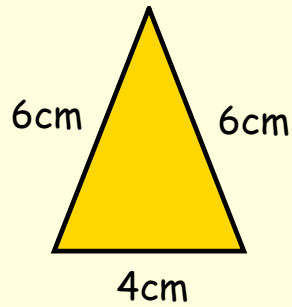
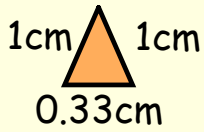
Example 3

The two triangles are similar. Find the missing lengths a and b .



Plenary

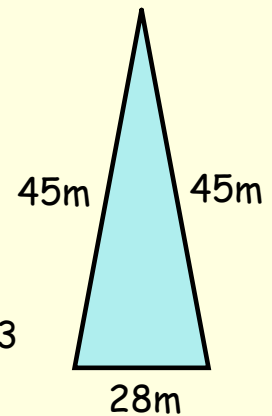
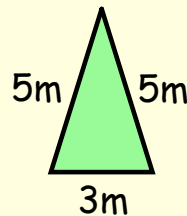
Which shapes are mathematically similar?



Starter

1) Are these triangles similar?

No as $3 \times 9 = 27$ not 28



2) How many roots does the graph of $y = x^2 - 8x + 13$

have? Discriminant = $13 > 0$

Therefore 2 Roots.

3) What is the distance between the points (2, 5) and (-8, 13)?

$$\sqrt{10^2 + 8^2} = \sqrt{164} \approx 12.9$$

Surface Area and Volume Scale Factors



Today we are learning...

The relationship between area and volume scale factors.

I will know if I have been successful if...

I have conducted an investigation on surface area scale factors.

I have conducted an investigation on volume scale factors.

I have shared my findings with others in the class.

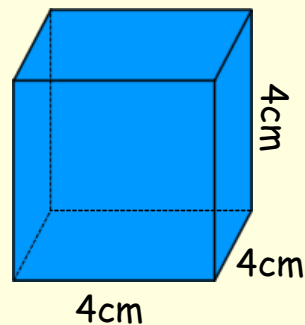
Surface Area and Volume

To find the surface area of a cube or cuboid...

$$4 \times 4 \times 6 = 96 \text{ cm}^2$$

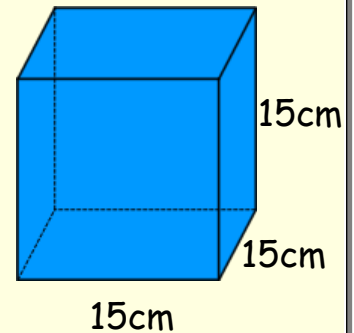
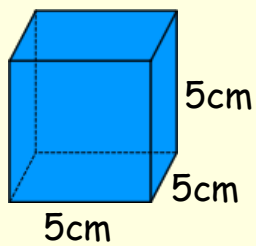
To find the volume of a cube or cuboid...

$$4 \times 4 \times 4 = 64 \text{ cm}^3$$



Investigation

When we enlarge a 3D object by a given scale factor, does the volume and the surface area also increase by the same scale factor?



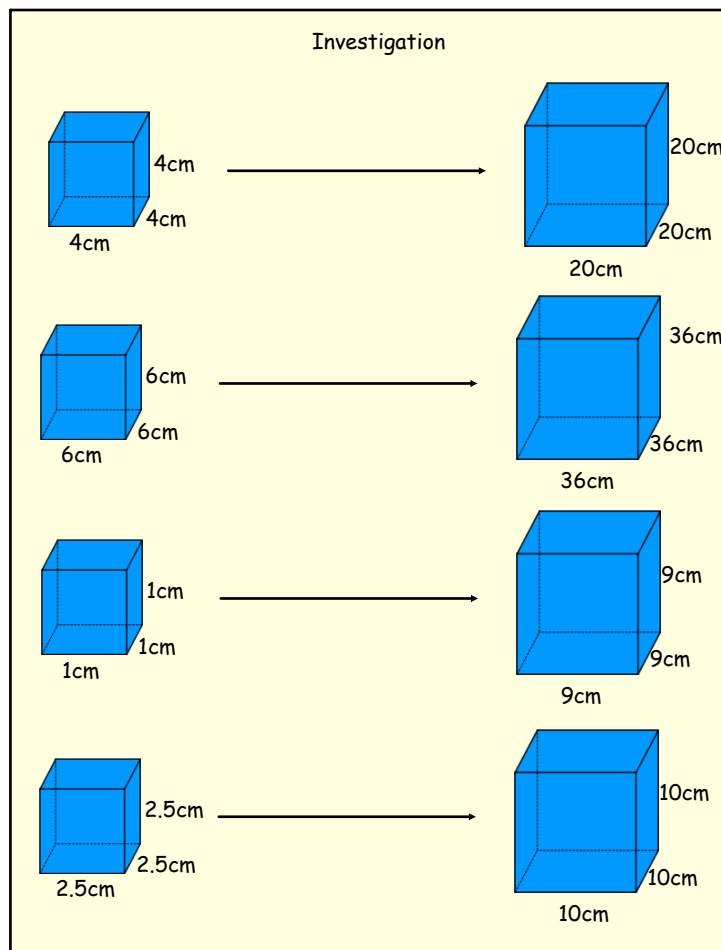
	Side Lengths	Surface Area	Volume
Small Cube	5cm	150cm ²	125cm ³
Large Cube	15cm	1350cm ²	3375cm ³
Scale Factor	3	9	27

$$k \quad k^2 \quad k^3$$

Investigation

When we enlarge a 3D object by a given scale factor, does the volume and the surface area also increase by the same scale factor?

No, but is there still a relationship?



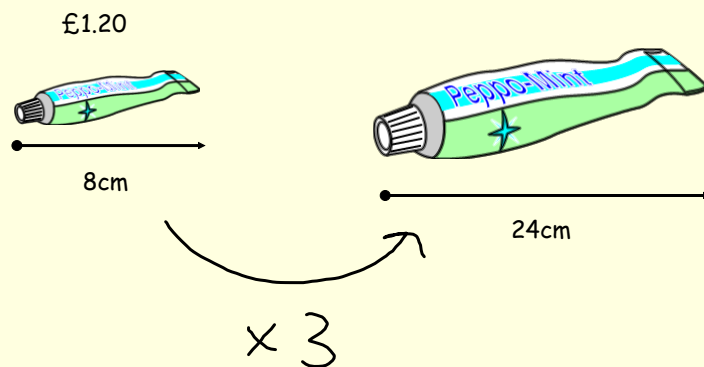
Investigation - Conclusion

When the length scale factor = k

The area scale factor = k^2

The volume scale factor = k^3

How much should the large tube cost?



$$\text{Volume s.f} = 3^3 = 27$$

$$£1.20 \times 27$$

$$= \pounds 32.40$$